

# Axions: Diversity beats Simplicity

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Work with R. Kappl and M. Winkler, (1) [arXiv:1503.01777](https://arxiv.org/abs/1503.01777), (2) to appear 1511.0XXXX



Bethe Center for  
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# Useful Axions

Axions can play a role for

- the strong CP problem in QCD (Peccei, Quinn, 1977)
- the mechanism of inflation (Freese, Frieman, Olinto, 1990)
- the source of quintessence (Frieman, Hill, Stebbins, Waga, 1995)

Axions are abundant in string theory constructions

- there is an opportunity for multi-axion systems
- that seems to be helpful for the consistency of axionic models
- two is better than one

**Vielfalt statt Einfalt: Diversity beats Simplicity**

# Outline

Concentrate here (CosPA 2015) on inflation

- axionic inflation
- Planck satellite and BICEP2 data
- high scale inflation and trans-Planckian excursions
- **the alignment of axions and its stability**
- the question of low scale Susy

Other application of multi-axion systems

- axionic domain walls for QCD axion (Choi, Kim, 1985)
- alignment of quintessential axions (Kaloper, Sorbo, 2006)

# The Quest for Flatness

The mechanism of inflation requires a “flat” potential.  
We demand

- symmetry reason for flatness of potential
- slightly broken symmetry to move the inflaton

The obvious candidate is **axionic inflation**

- axion has only derivative couplings to all orders in perturbation theory
- broken by non-perturbative effects (instantons)

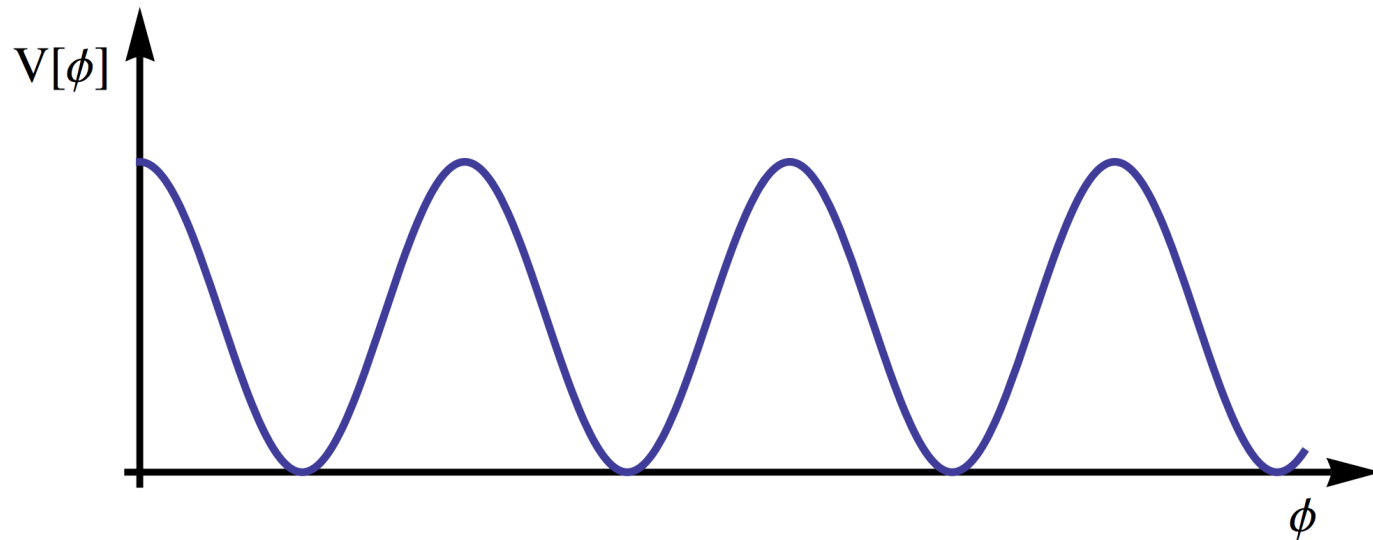
Motivated by the QCD axion

(Freese, Frieman, Olinto, 1990)

# The Axion Potential

The axion exhibits a shift symmetry  $\phi \rightarrow \phi + c$

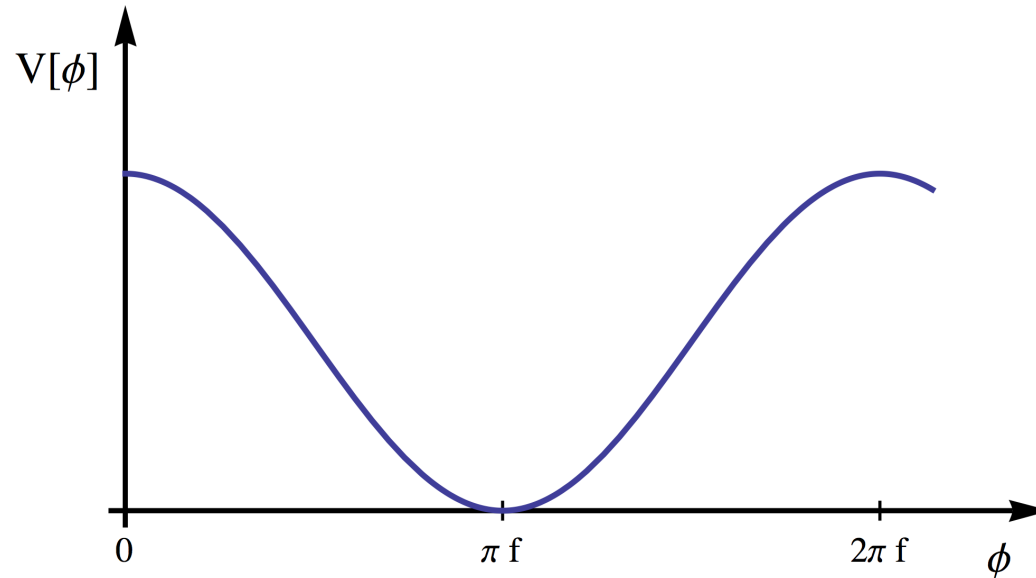
Nonperturbative effects break this symmetry to a remnant **discrete shift symmetry**



$$V(\phi) = \Lambda^4 \left[ 1 + \cos \left( \frac{2\pi\phi}{f} \right) \right]$$

# The Axion Potential

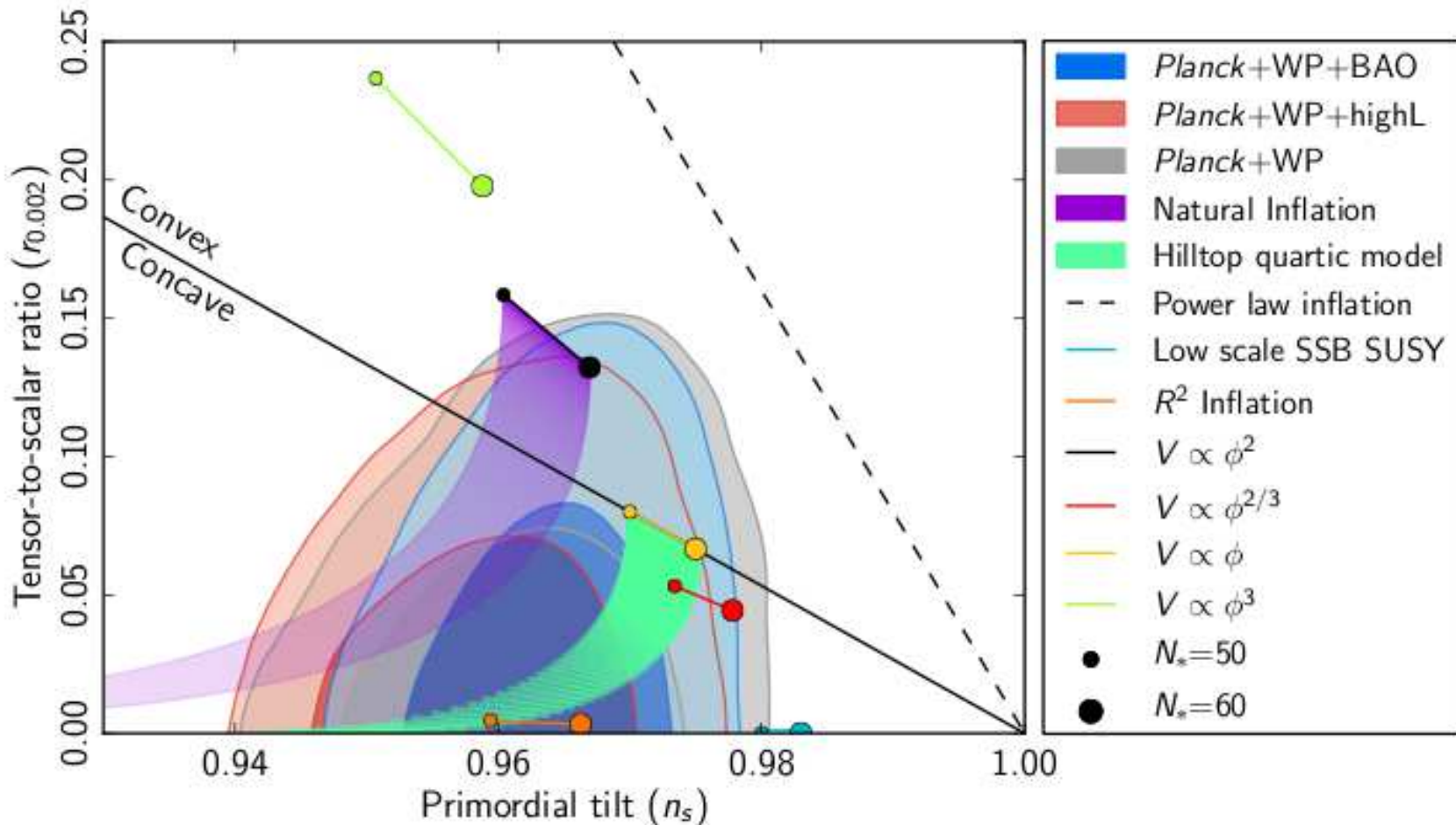
Discrete shift symmetry identifies  $\phi = \phi + 2\pi n f$



$$V(\phi) = \Lambda^4 \left[ 1 + \cos \left( \frac{2\pi\phi}{f} \right) \right]$$

$\phi$  confined to one fundamental domain

# Planck results (Spring 2013)



# BICEP2 (Spring 2014)

Tentatively large tensor modes of order  $r \sim 0.1$  had been announced by the BICEP collaboration

- large tensor modes brings us to scales of physics close to the Planck scale and the so-called “Lyth bound”
- potential  $V(\phi)$  of order of GUT scale  $\text{few} \times 10^{16} \text{ GeV}$
- trans-Planckian excursions of the inflaton field
- For a quadratic potential  $V(\phi) \sim m^2 \phi^2$  it implies  $\Delta\phi \sim 15M_{\text{P}}$  to obtain 60 e-folds of inflation

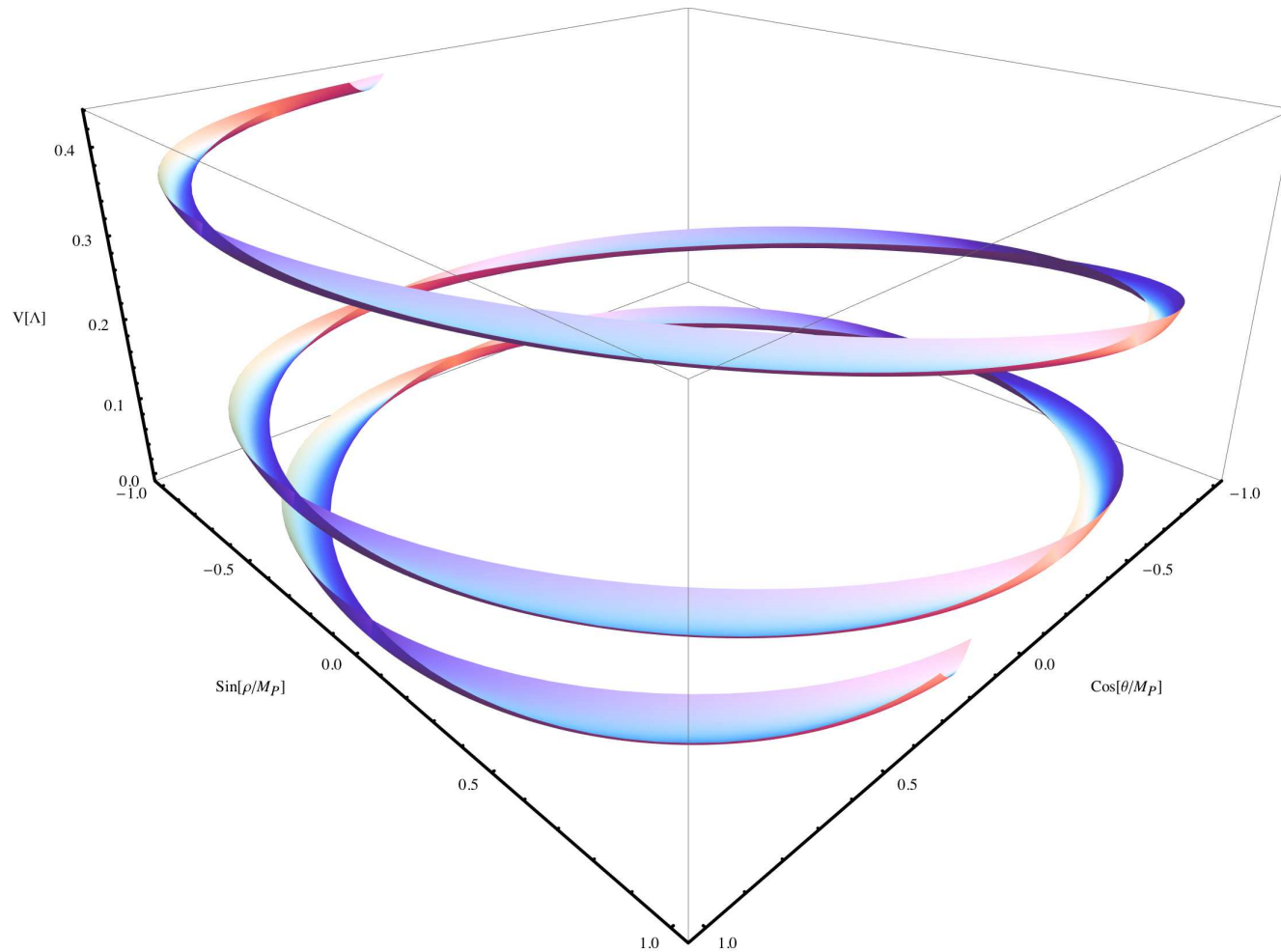
Axionic inflation, on the other hand, seems to require the decay constant to be limited:  $f \leq M_{\text{P}}$ .

So this might be problematic.

(Banks, Dine, Fox, Gorbatov, 2003)



# Solution



Helical motion of one axion in the potential of a second one

# Aligned axions

A way out is the consideration of two (or more) fields.

(Kim, Nilles, Peloso, 2004)

- top-down approach favours a multi-axion picture
- we require  $f \leq M_{\text{P}}$  for the individual axions
- **diversity beats simplicity**

The alignment prolongs the fundamental domain of the aligned axion to super-Planckian values, as the axionic inflaton spirals down in the potential of the second axion

Alternative mechanisms, like e.g. "Axion Monodromy" give a similar qualitative picture

(McAllister, Siverstein, Westphal, 2008)

# The KNP set-up

We consider two axions

$$\mathcal{L}(\theta, \rho) = (\partial\theta)^2 + (\partial\rho)^2 - V(\rho, \theta)$$

with potential

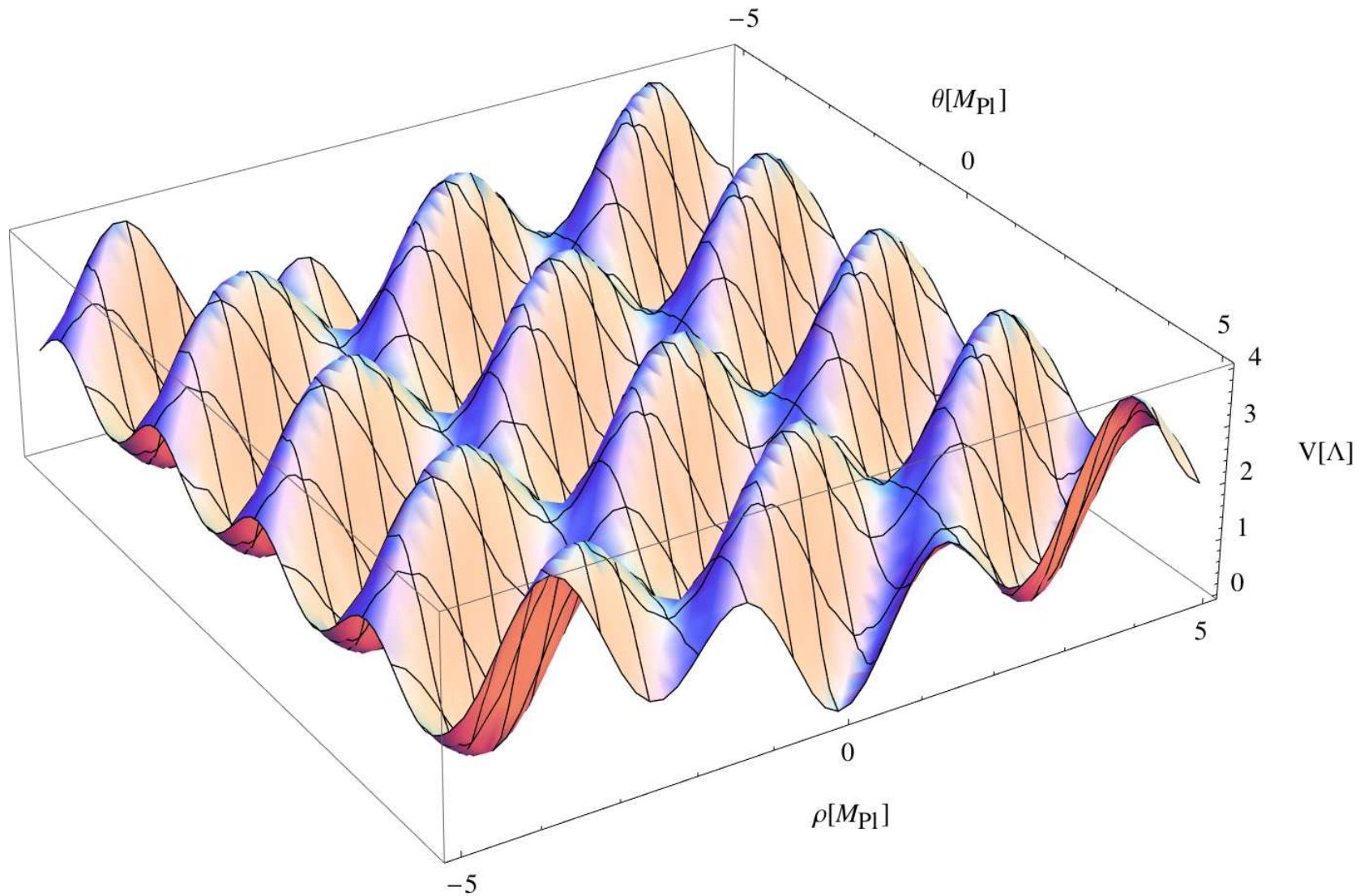
$$V(\theta, \rho) = \Lambda^4 \left( 2 - \cos \left( \frac{\theta}{f_1} + \frac{\rho}{g_1} \right) - \cos \left( \frac{\theta}{f_2} + \frac{\rho}{g_2} \right) \right)$$

This potential has a flat direction if  $\frac{f_1}{g_1} = \frac{f_2}{g_2}$

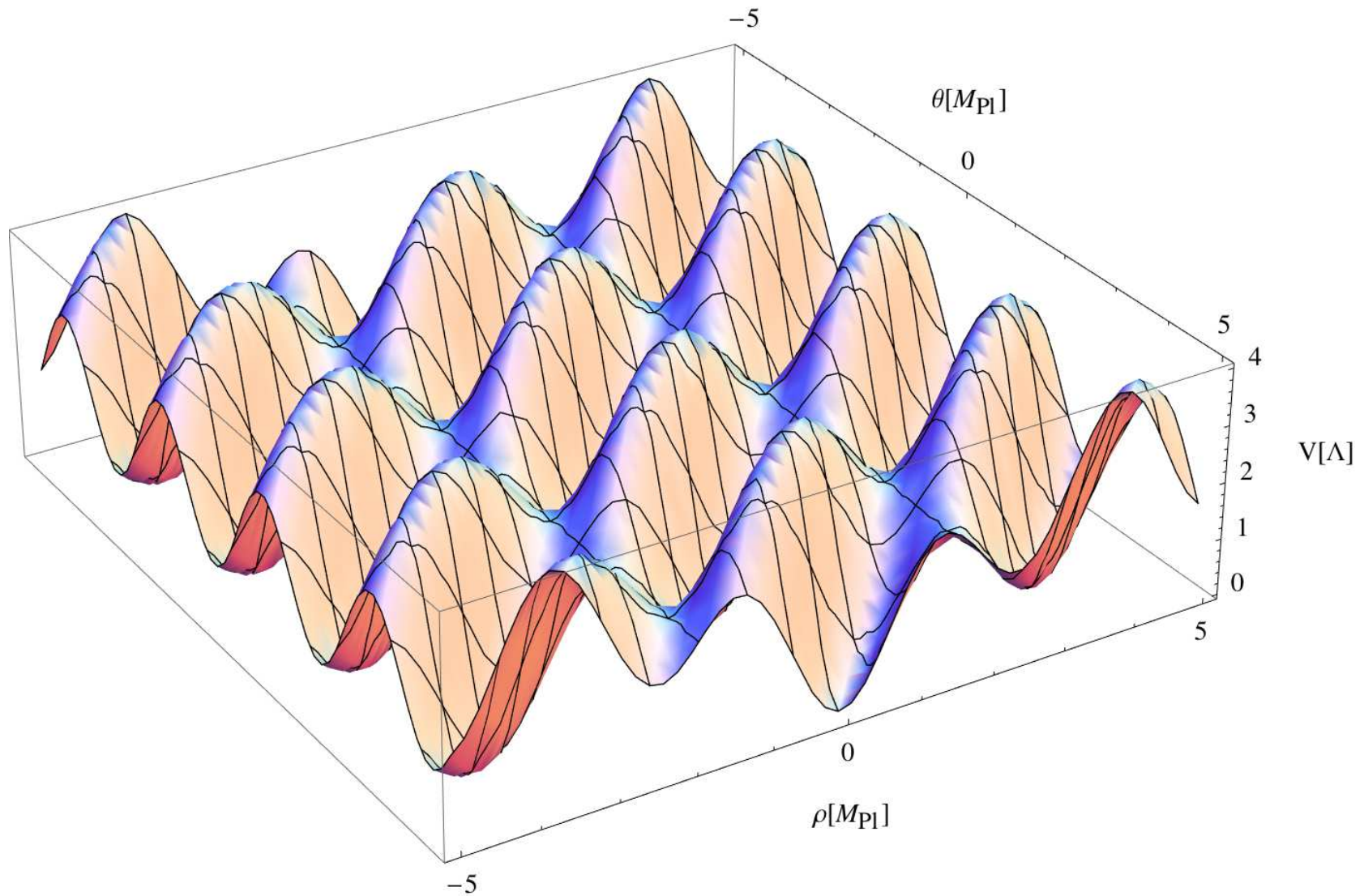
Alignment parameter defined through  $\alpha = g_2 - \frac{f_2}{f_1} g_1$

For  $\alpha = 0$  we have a massless field  $\xi$ .

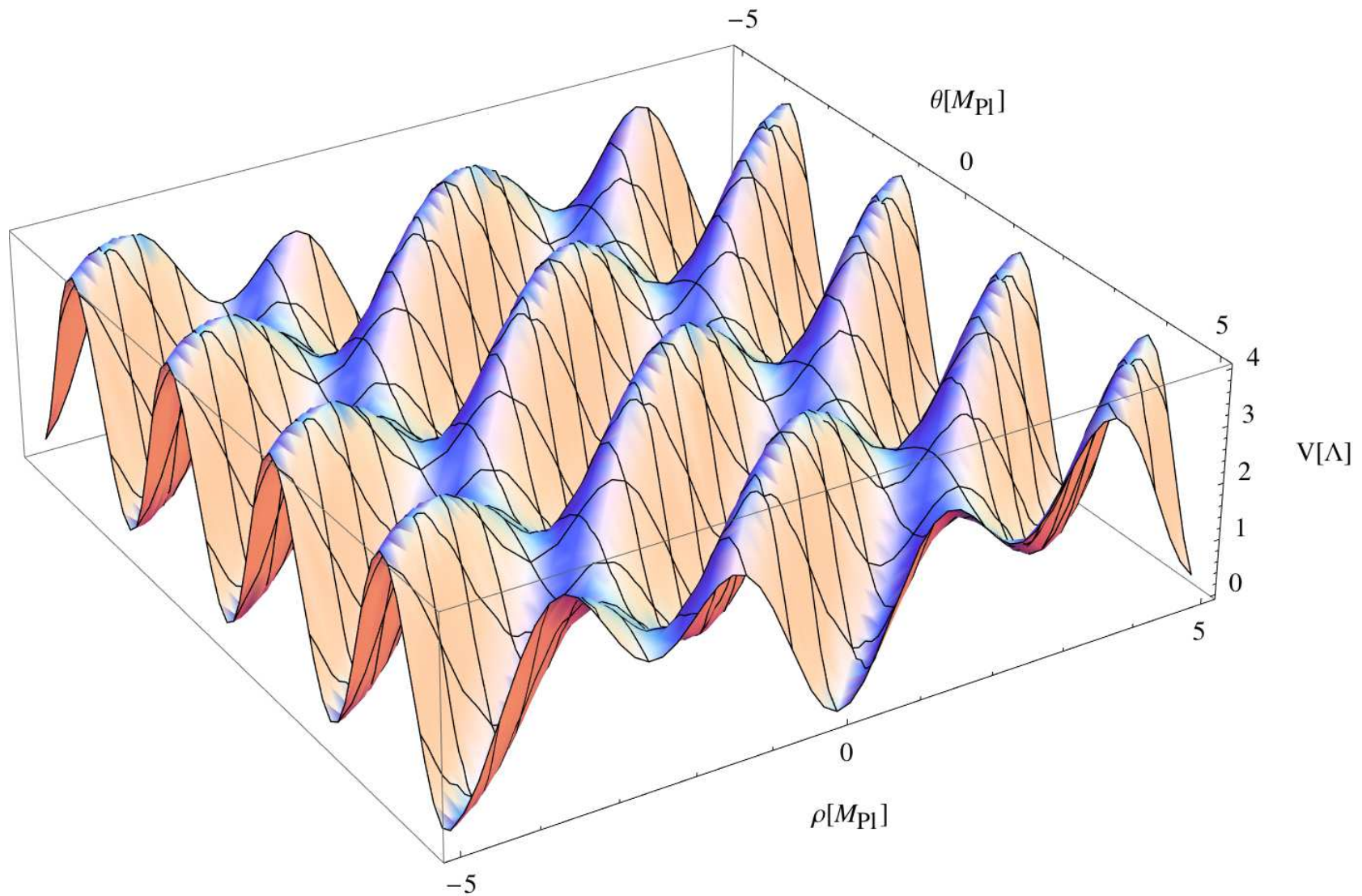
# Potential for $\alpha = 1.0$



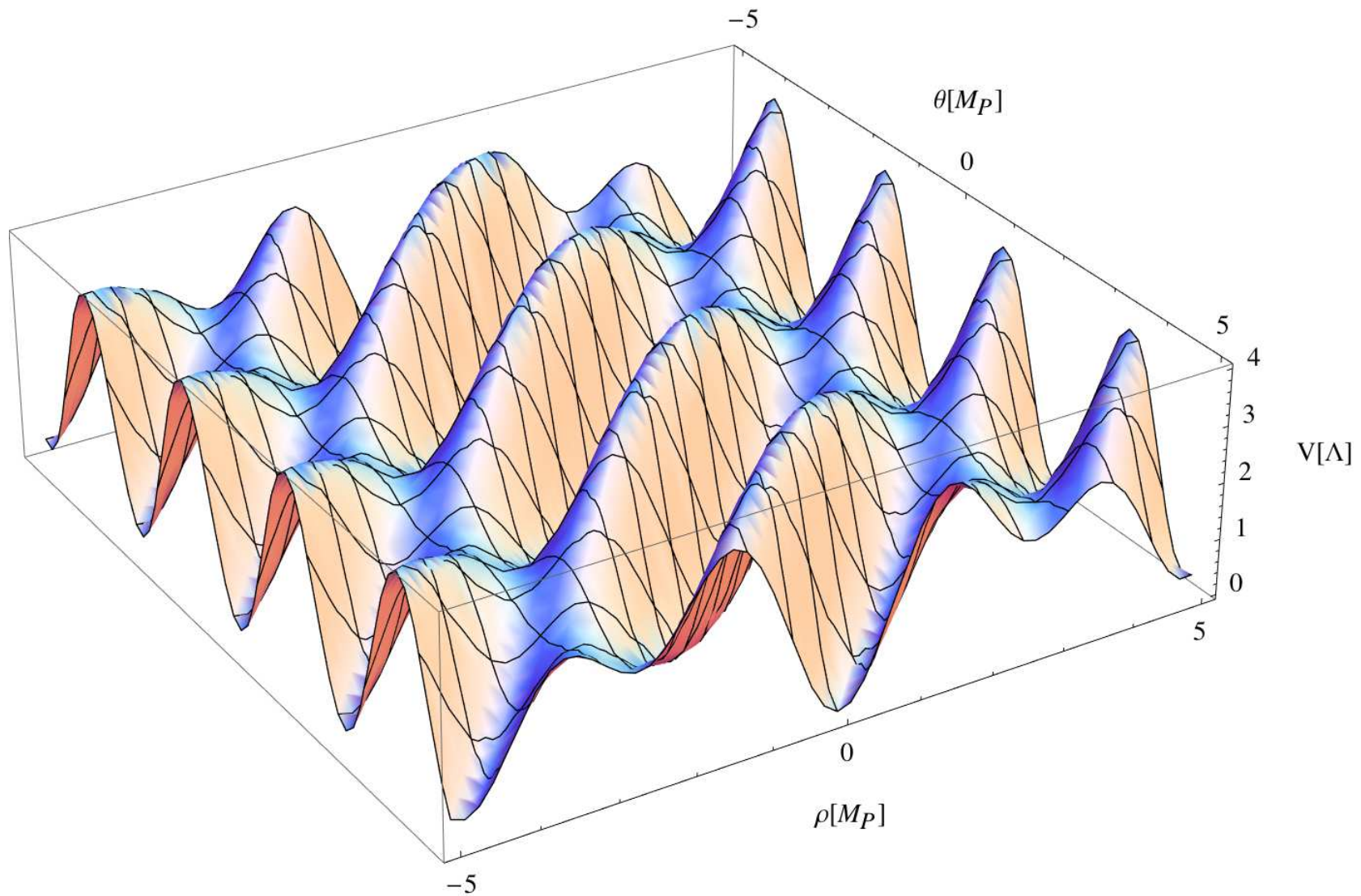
# Potential for $\alpha = 0.8$



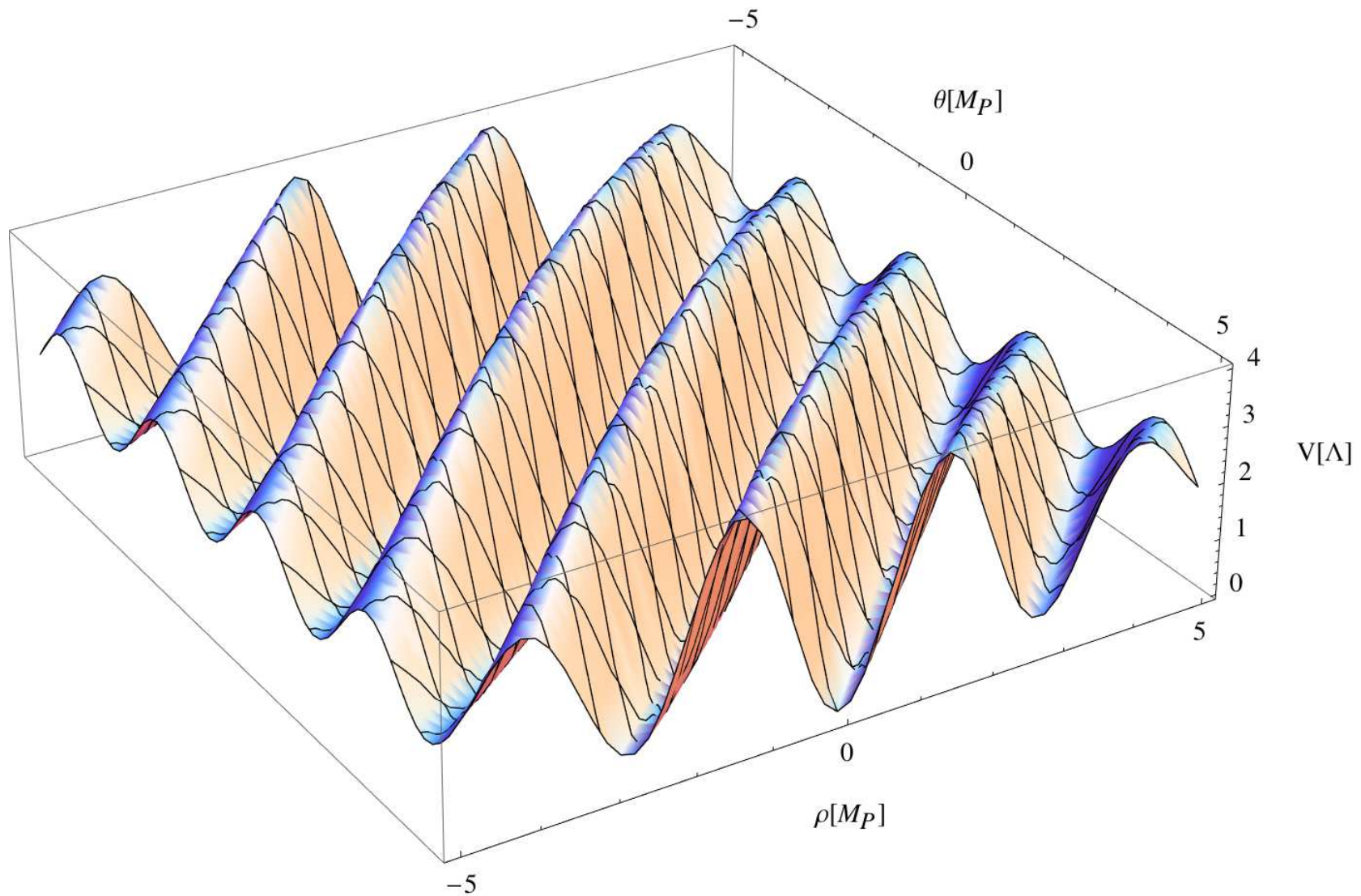
# Potential for $\alpha = 0.5$



# Potential for $\alpha = 0.3$

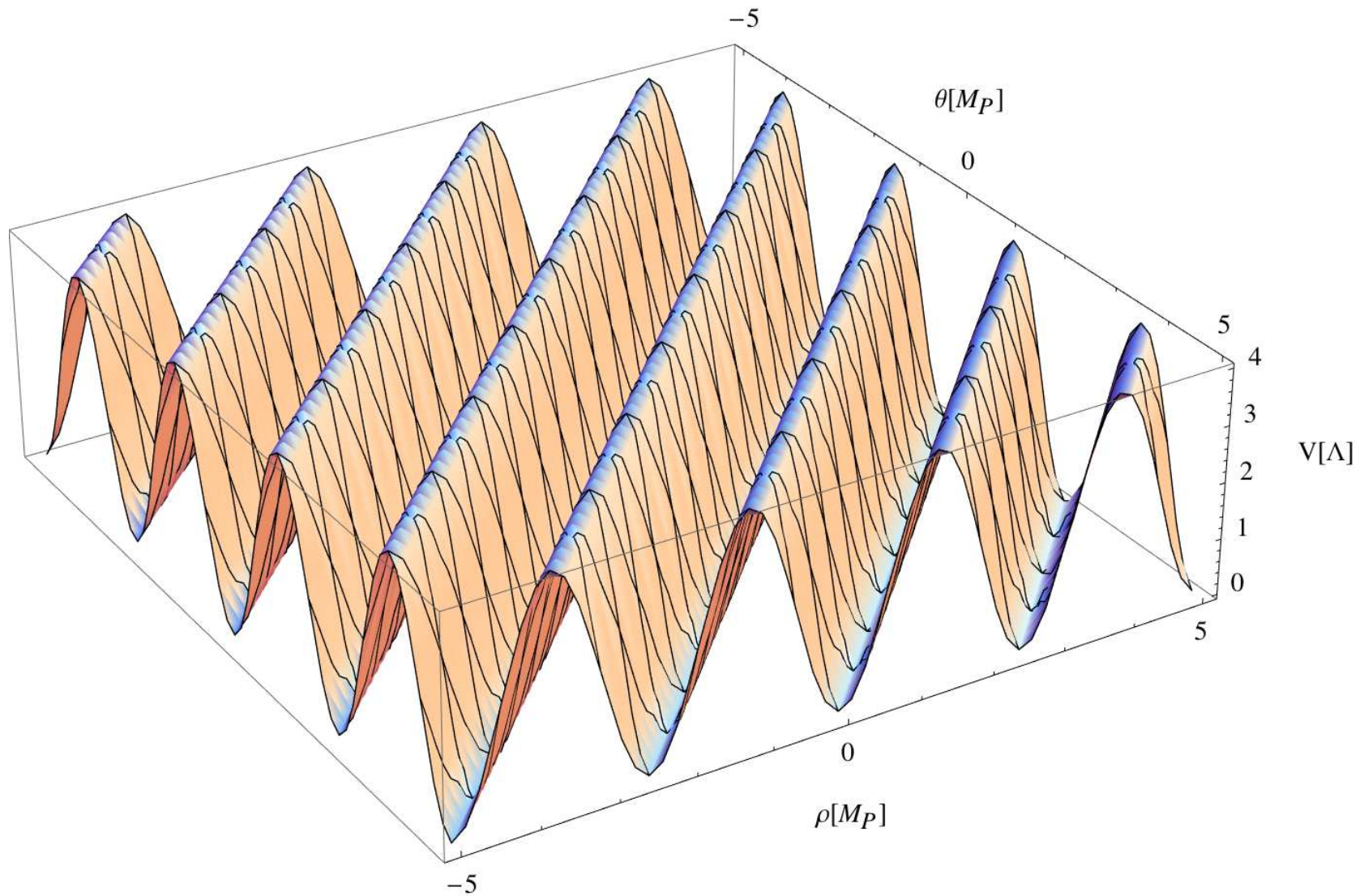


# Potential for $\alpha = 0.1$





# Potential for $\alpha = 0$



# The lightest axion

Mass eigenstates are denoted by  $(\xi, \psi)$ . The mass eigenvalues are

$$\lambda_{1/2} = F \pm \sqrt{F^2 + \frac{2g_1g_2f_1f_2 - f_2^2g_1^2 - f_1^2g_2^2}{f_1^2f_2^2f_1^2g_2^2}}$$

with 
$$F = \frac{g_1^2g_2^2(f_1^2 + f_2^2) + f_1^2f_2^2(g_1^2 + g_2^2)}{2f_1^2f_2^2g_1^2g_2^2}$$

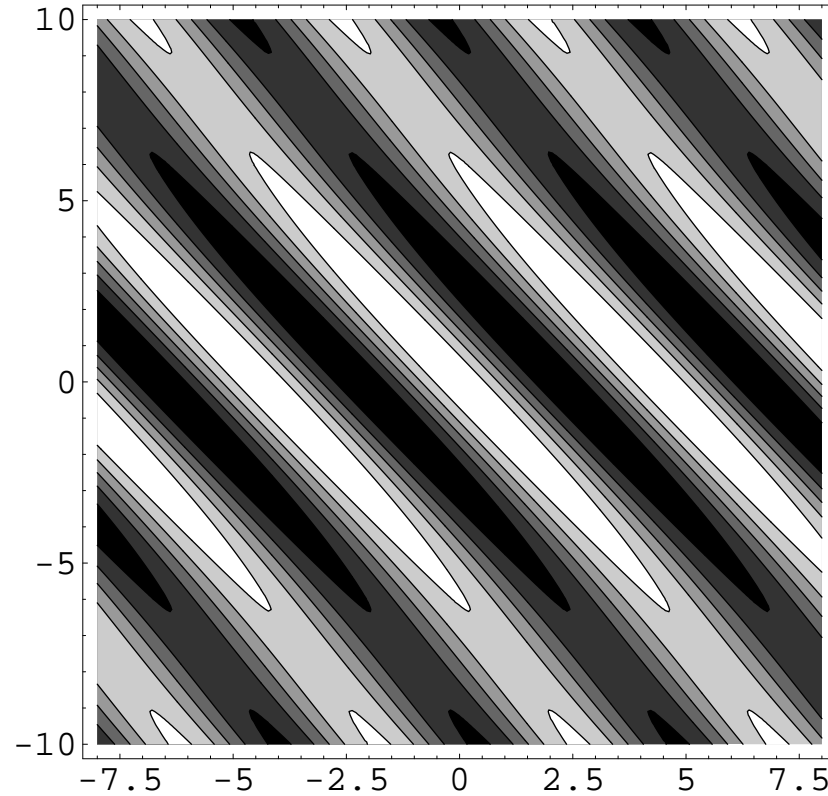
Lightest axion  $\xi$  has potential

$$V(\xi) = \Lambda^4 [2 - \cos(m_1(f_i, g_1, \alpha)\xi) - \cos(m_2(f_i, g_1, \alpha)\xi)]$$

leading effectively to a **one-axion system**

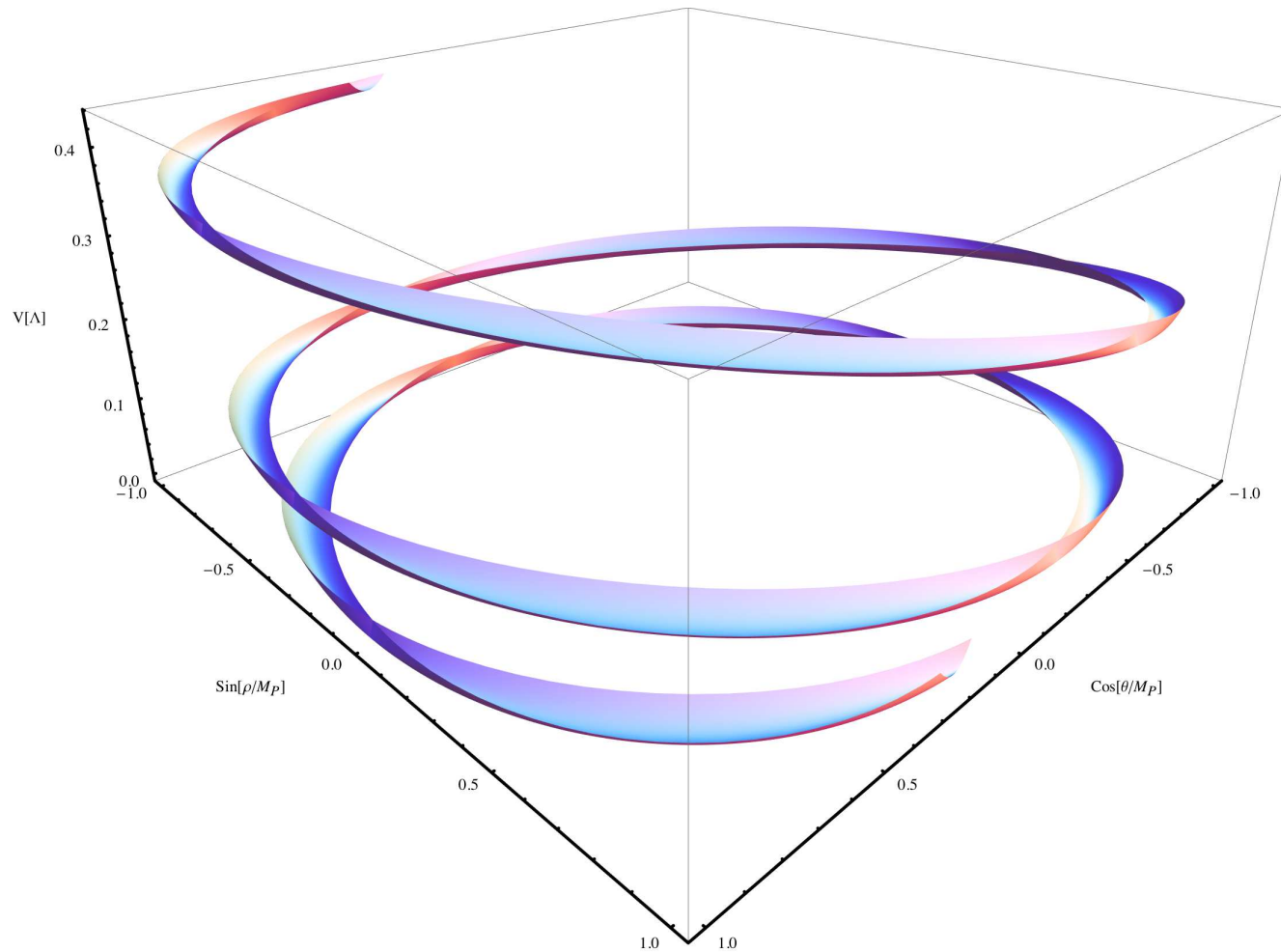
$$V(\xi) = \Lambda^4 \left[ 1 - \cos\left(\frac{\xi}{\tilde{f}}\right) \right] \quad \text{with} \quad \tilde{f} = \frac{f_2g_1\sqrt{(f_1^2 + f_2^2)(f_1^2 + g_1^2)}}{f_1^2\alpha}$$

# Axion landscape of KNP model



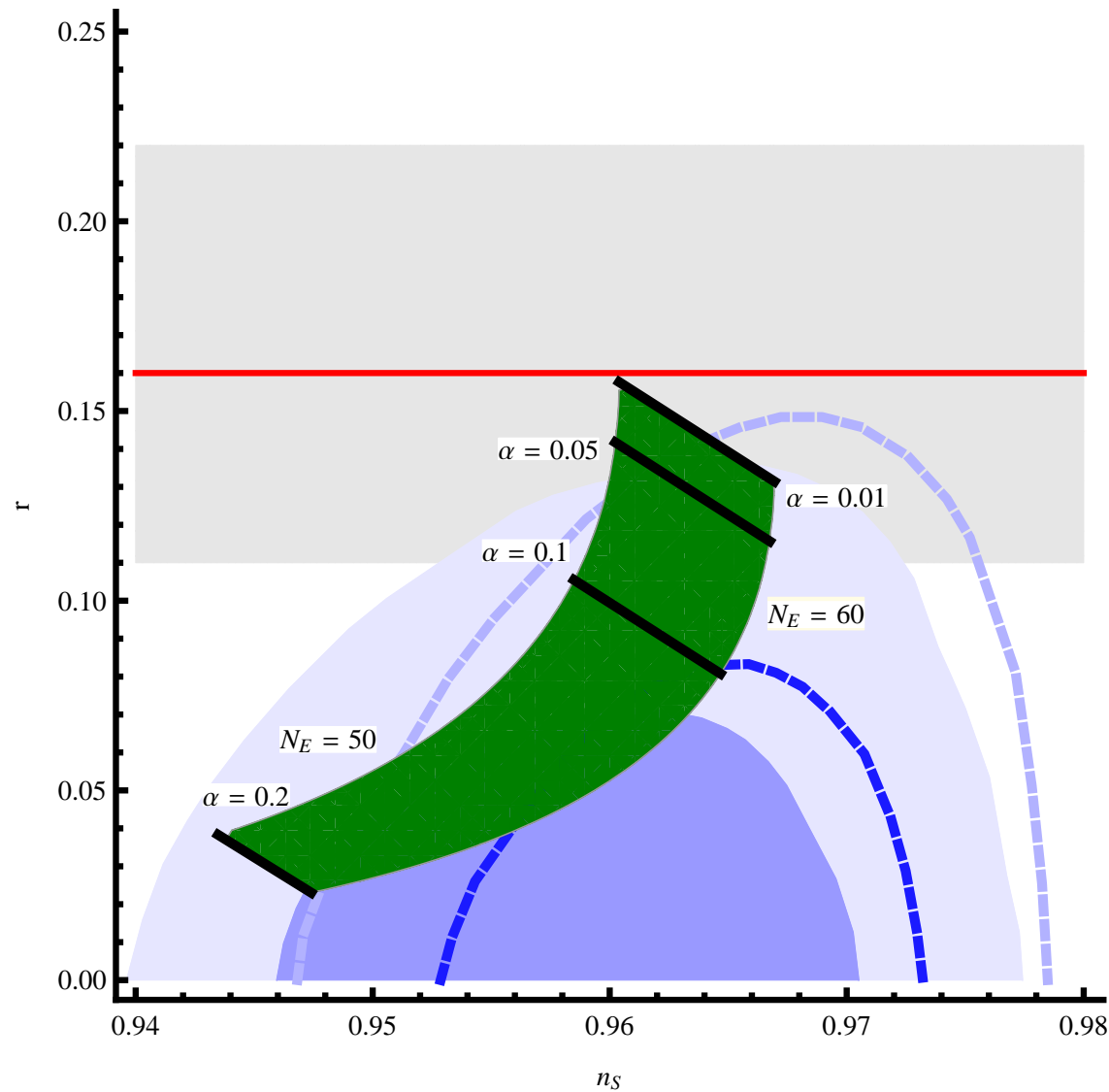
The field  $\xi$  rolls within the valley of  $\psi$ . The motion of  $\xi$  corresponds to a motion of  $\theta$  and  $\rho$  over **many cycles**. The system is still controlled by discrete symmetries.

# Monodromic Axion Motion



One axion spirals down in the valley of a second one.

# The “effective” one-axion system



# UV-Completion

Large tensor modes and  $\Lambda \sim 10^{16}$  GeV lead to theories at the “edge of control” and require a reliable UV-completion

- small radii
- large coupling constants
- light moduli might spoil the picture

# UV-Completion

Large tensor modes and  $\Lambda \sim 10^{16}$  GeV lead to theories at the “edge of control” and require a reliable UV-completion

- small radii
- large coupling constants
- light moduli might spoil the picture

So it is important to find reliable symmetries

- axions are abundant in string theory
- perturbative stability of “shift symmetry”
- broken by nonperturbative effects
- potential protection through supersymmetry

# The Quest for Supersymmetry

So far our discussion did not consider supersymmetry.

- How to incorporate axion inflation in a Susy-framework?
- A possible set-up for natural inflation would be

$$W = W_0 + A \exp(-a\rho); \quad K \sim (\rho + \bar{\rho})^2$$

For a simple form of axionic inflation we have to assume that  $W_0$  dominates in the superpotential

- this implies that Susy is broken at a large scale
- Does high scale inflation require high scale Susy breakdown?

Previous constructions point towards high scale Susy!



# Stabilizer fields

Toy model: quadratic inflation in supergravity

$$W = \frac{1}{2}m\rho^2, \quad K = \frac{(\bar{\rho} + \rho)^2}{4}$$

where the inflaton corresponds to  $\text{Im}(\rho)$

**Problem:** Potential is unbounded from below because of the supergravitational term  $-3|W|^2$

**Solution:** introduce a stabilizer field  $X$

$$W = mX\rho, \quad K = \frac{(\bar{\rho} + \rho)^2}{4} + k(|X|^2) - \frac{|X|^4}{\Lambda^2}$$

(Kawasaki, Yamaguchi, Yanagida, 2000)

# Susy and Natural Inflation

Axionic inflation with a stabilizer field  $X$ .

$$W = m^2 X (e^{-a\rho} - \lambda), \quad K = \frac{(\bar{\rho} + \rho)^2}{4} + k(|X|^2) - \frac{|X|^4}{\Lambda^2}$$

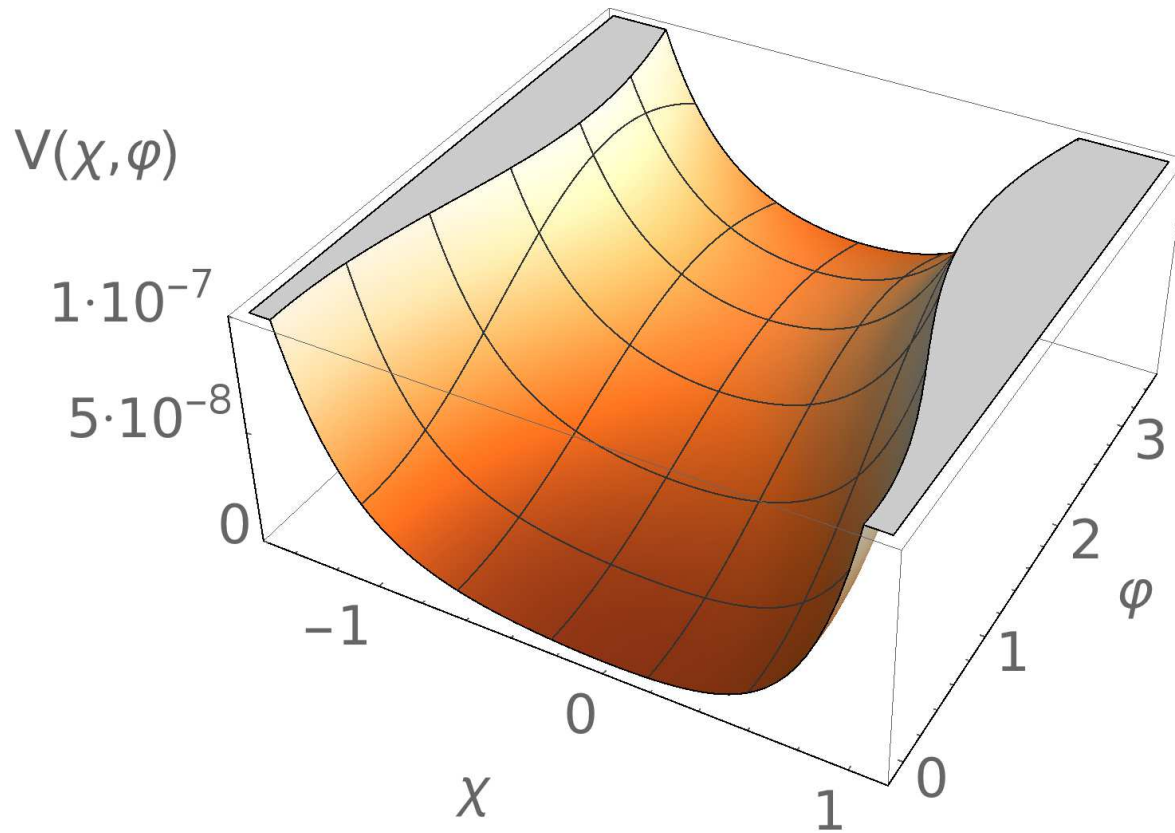
Supersymmetric ground state at  $X = 0, \rho = \rho_0 = -\log(\lambda)/a$

$$V = \frac{m^4 e^{-a(2\rho_0 + \chi)}}{\rho_0 + \chi} [\cosh(a\chi) - \cos(a\varphi)]$$

Susy is restored at the end of inflation.

**Conclusion: additional fields help to incorporate Susy.**

# Trapped Saxion



The axion-saxion valley

# Towards string theory

String theory contains many (moduli and matter) fields and stabilizers can be easily incorporated.

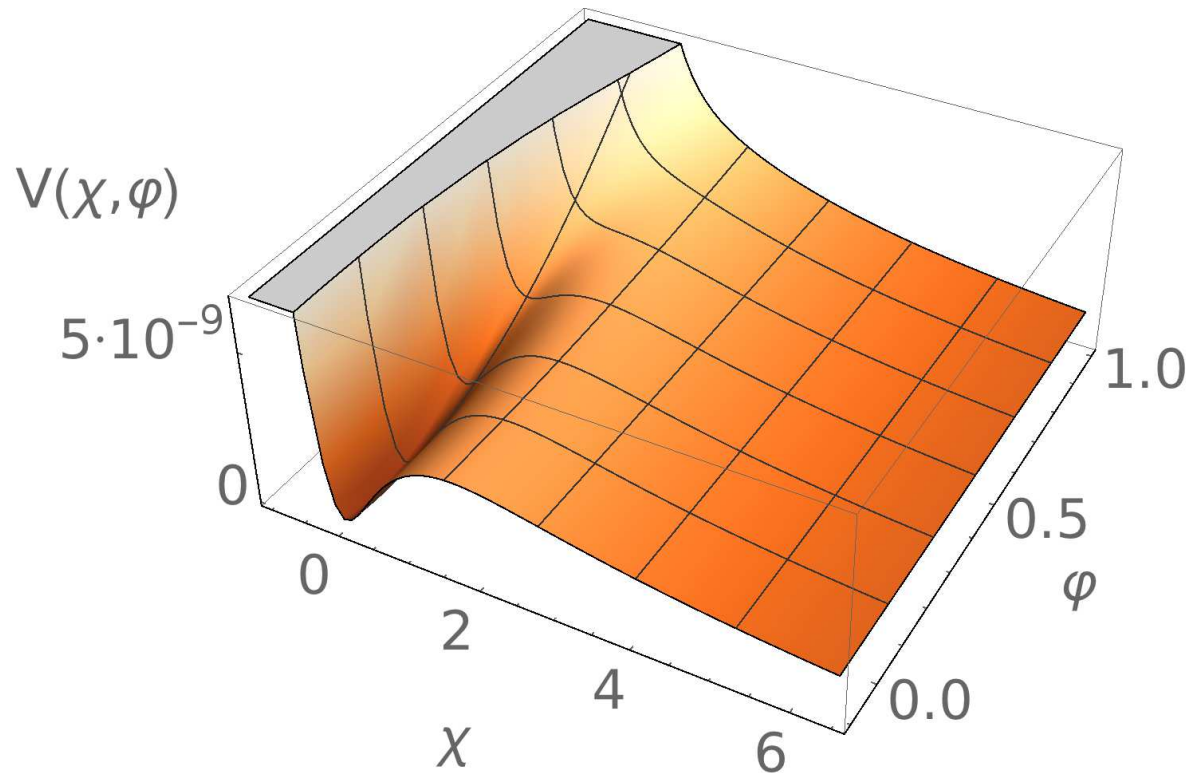
Challenge: we typically have  $K = -\log(\rho + \bar{\rho})$  leading to

$$V = \frac{m^4 e^{-a(2\rho_0 + \chi)}}{\rho_0 + \chi} [\cosh(a\chi) - \cos(a\varphi)] .$$

This destabilises the saxion field  
(in the presence of low scale supersymmetry).

**A successful model has to address the stabilisation of moduli fields.**

# Unstable Saxon



Potential run-off of saxion.

**We need more fields to stabilise the system.**

# A String Scenario

We have to achieve moduli fixing and trans-Planckian excursion of the inflaton field

- alignment of axions
- stabilisation of saxions and other moduli

This can be done with the help of flux superpotentials, gauge- and world-sheet-instantons (e.g. with magnetised D-branes in toroidal/orbifold compactification)

$$W = W_{\text{flux}} + \sum_i A_i e^{-2\pi n_i^\beta T_\beta} + \prod_i \phi_i e^{-S_{\text{inst}}(T_\beta)},$$

Still we have to make an effort to avoid high scale Susy.

(Kappl, Nilles, Winkler(1), 2015; Ruehle, Wieck, 2015)

# A Benchmark Model

Again we need more fields.

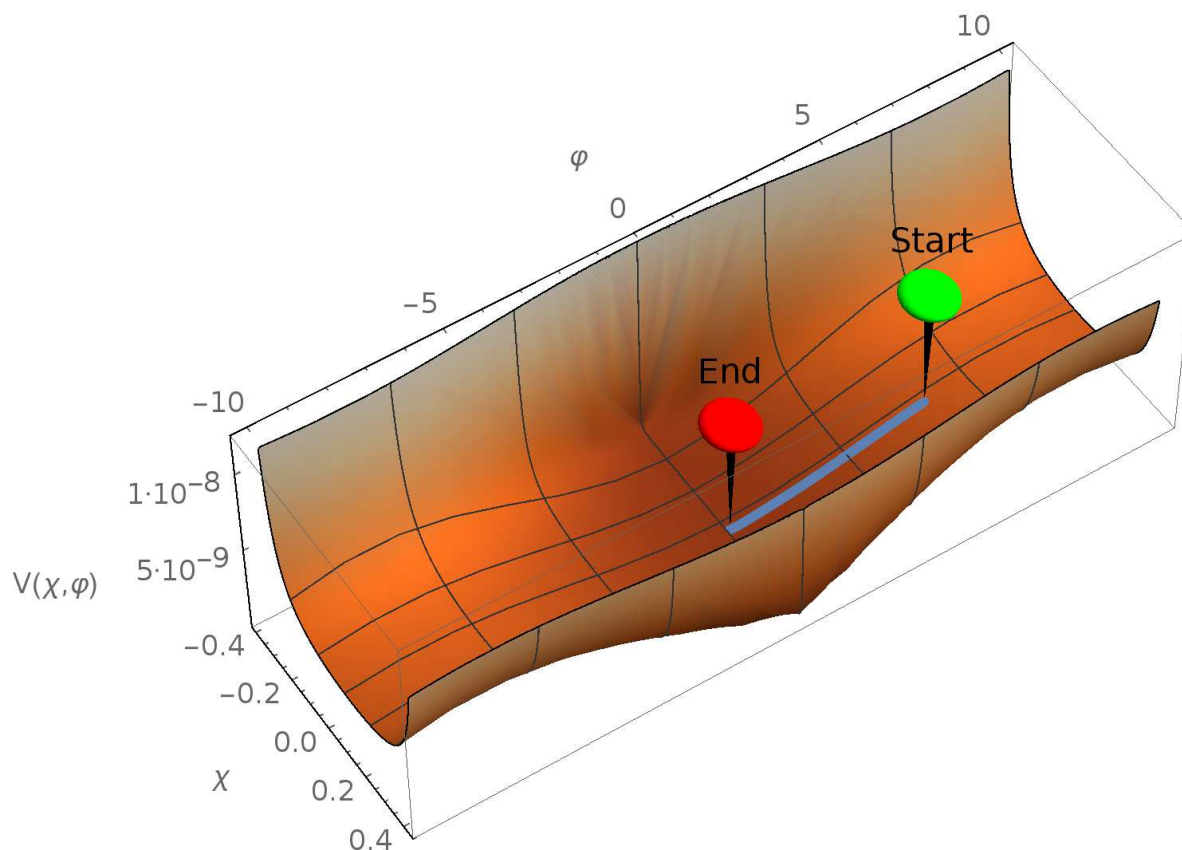
$$W = \sum_{i=1}^2 m_i^2 X_i (e^{-a_i \rho_1 - b_i \rho_2} - \lambda_i)$$

With two axions and stabilizer fields we can achieve

- a susy ground state at  $X_{1,2} = 0$
- one heavy and one light combination of  $\rho_i = \chi_i + i\varphi_i$

$$V = \frac{\lambda_1^2 m_1^4 e^{-\delta\chi} [\cosh(\delta\chi) - \cos(\delta\varphi)]}{2(\rho_{1,0} + b_2\chi)(\rho_{2,0} - a_2\chi)}$$

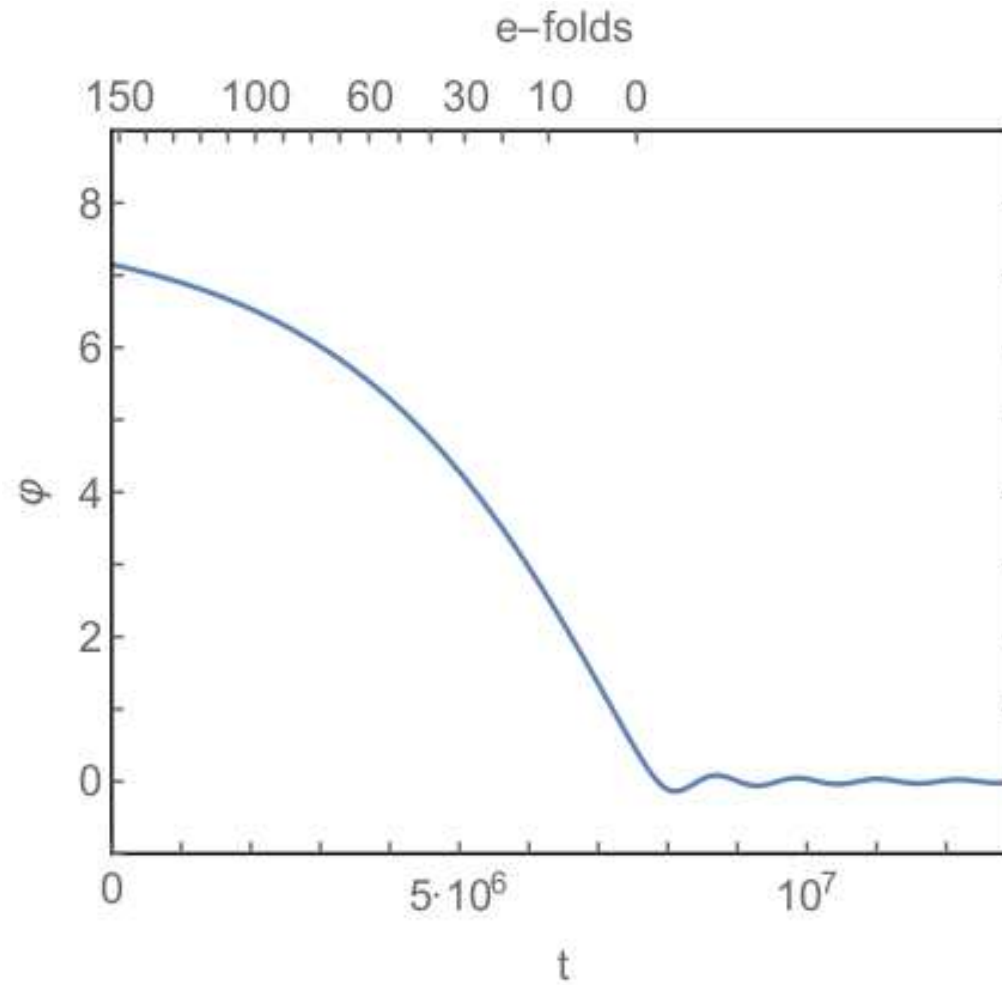
# Aligned Axion with Trapped Saxion



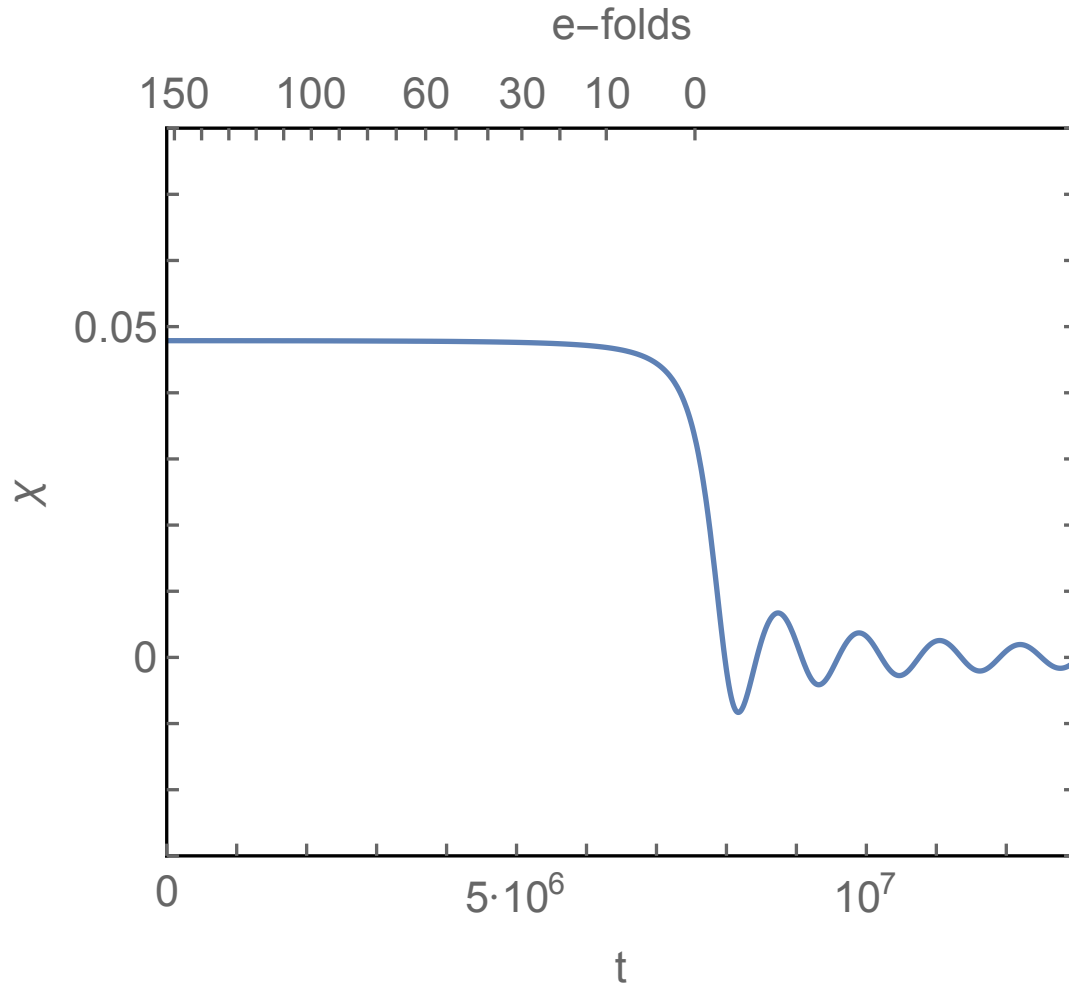
The valley is narrow (observe difference of scales)



# Evolution of Axion



# Evolution of Saxion



The saxion stays close to zero

# Comparison with observations

In the extreme case, again, we have an **effective one-axion** system with allowed trans-Planckian excursion.

But the other moduli and matter fields

- can influence the inflationary potential
- and might e.g. lead to a **flattening of the potential**

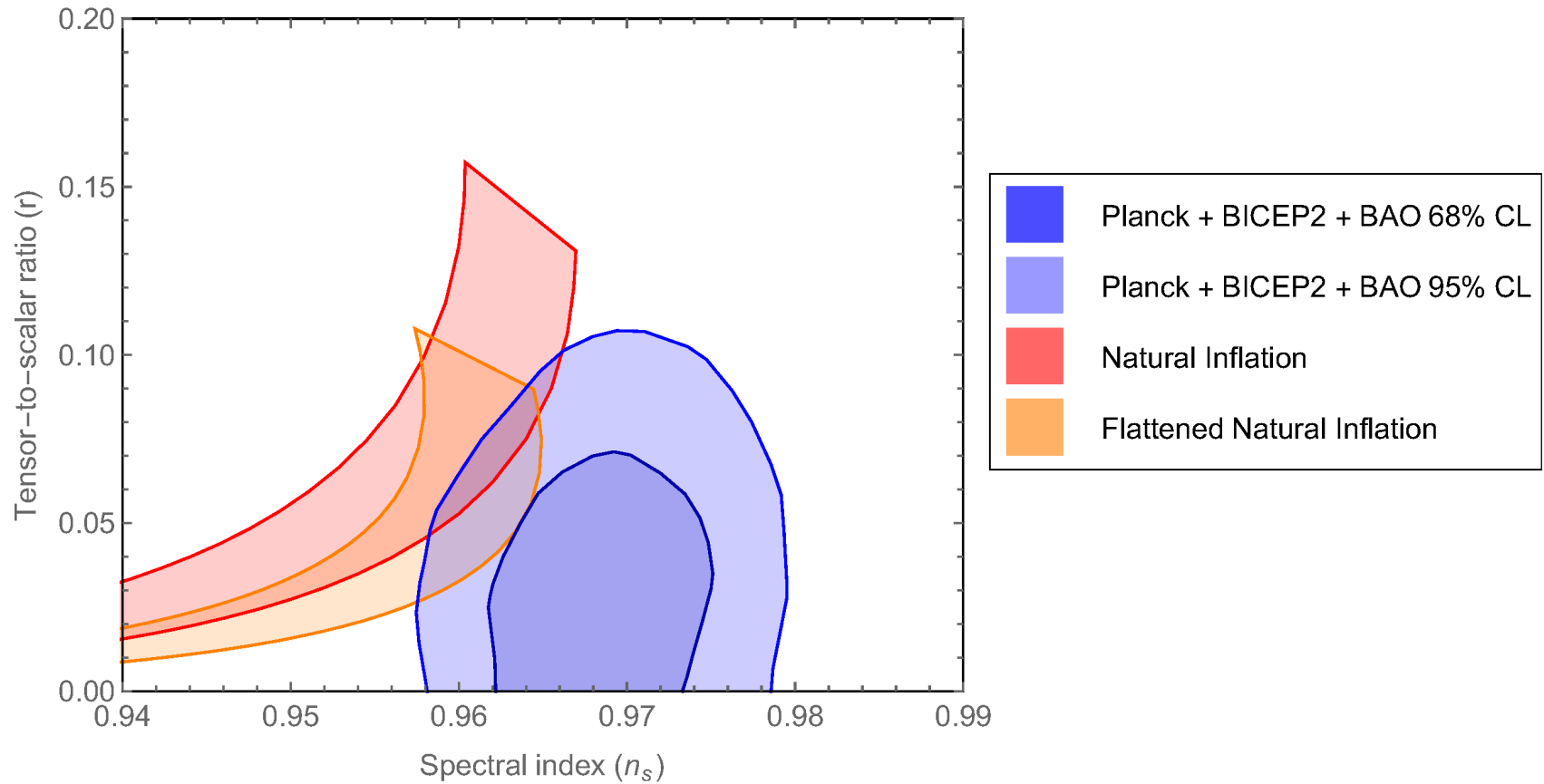
Comparison with data leads to an effective axion scale

$$f_{\text{eff}} \geq f_{\text{ew}} \times M_{\text{Planck}}$$

Other limits give a stronger influence of the additional axions and allow a **broader range of values in the  $n_s$ - $r$  plane**

(Peloso, Unal, 2015; Kappl, Nilles, Winkler(2), 2015)

# $n_s - r$ plane



(Kappl, Nilles, Winkler(1), 2015)

# Axionic inflation and supersymmetry

High scale inflation prefers large scale susy breakdown.  
The quest for low scale supersymmetry requires

- additional fields and a specific form of moduli stabilization.

The alignment of axions

- allows trans-Planckian excursions of the inflaton field,
- favours the appearance of low energy supersymmetry.

A satisfactory and consistent scheme require more fields:

**Diversity beats Simplicity**

# Stability

We have a very flat direction and within the effective QFT we are at the “edge of control”

- is inflation perturbed by other effects?
- is there an upper limit on  $f_{\text{eff}}$ ?

Remember that in case of a single axion we had limits

- $f_{\text{eff}} \leq M_{\text{string}}$  (Banks, Dine, Fox, Gorbатов, 2003)
- derived from dualities in string theory

In the multi-axion case these arguments are not directly applicable, but the question of trans-Planckian values should be tested in a given model

# Weak Gravity Conjecture (WGC)

It is based on prejudice about black hole properties and is formulated to constrain  $U(1)$  gauge interactions

(Arkani-Hamed, Motl, Nicolis, Vafa, 2006)

- give limits on mass to charge ratio  $q/m > 1$
- “convex hull” restrictions in multi-field case

But our “knowledge” on black hole properties (no-hair conjecture and information paradox) has changed recently

- fuzzballs, (Mathur, 2009-2015)
- brick- and fire-walls (Almheiri, Marolf, Polchinski, Sully, 2012)

The motivation for the WGC might not be valid any longer.

# WGC II

It is conjectured that the WGC (if true) might be applicable to axions (Rudelius, 2015)

- based on a chain of string dualities
- might give an upper limit on decay constants  $f_{\text{eff}}$

This might lead to a no-go theorem for large axion decay constants, but

- there are loop-holes in the presence of subleading instantons (Brown, Cottrell, Shiu, Soler, 2015)
- computationally we are at the “edge of control”

Needs to be clarified in explicit constructions.

(Kappl, Nilles, Winkler(2), 2015)



# Explicit String Constructions

In string theory we do not just get cosine potentials, but have to deal with modular functions (Jacobi theta- and/or Dedekind-functions), as e.g. in the case of

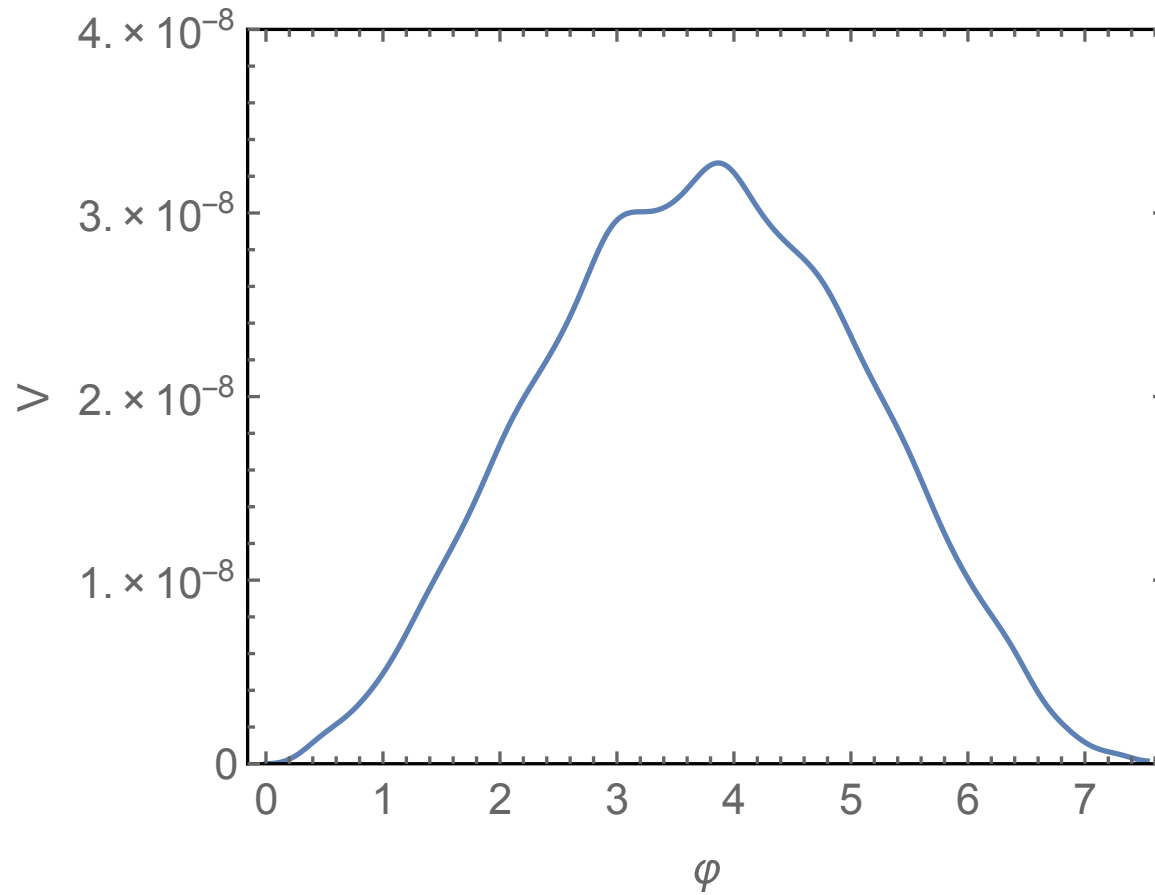
- world sheet instanton effects
- gauge kinetic functions and gaugino condensates

So we might consider instead

$$\eta(T) = e^{-\pi T/12} \times \prod_k (1 - e^{-2k\pi T})$$

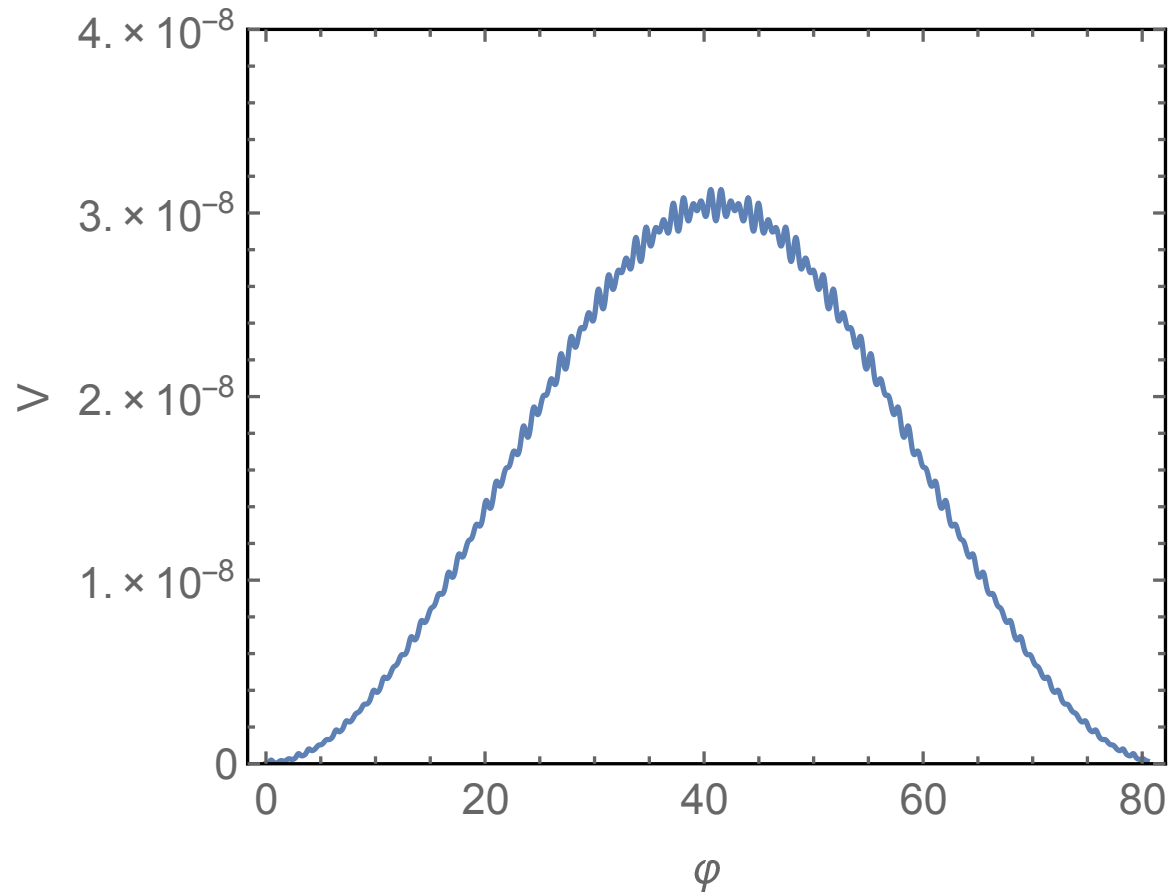
Higher harmonics give wiggles in the potential that perturb the flat direction and might stop inflation

# Wiggles



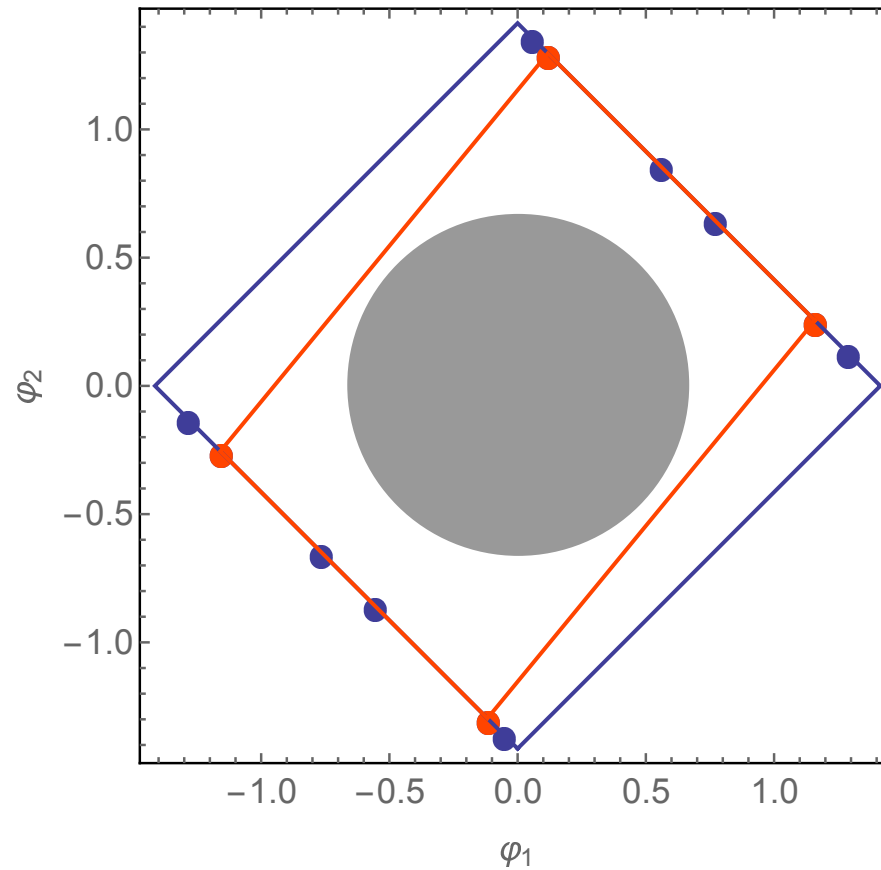
The wiggles in the case of weak alignment

# Wiggles



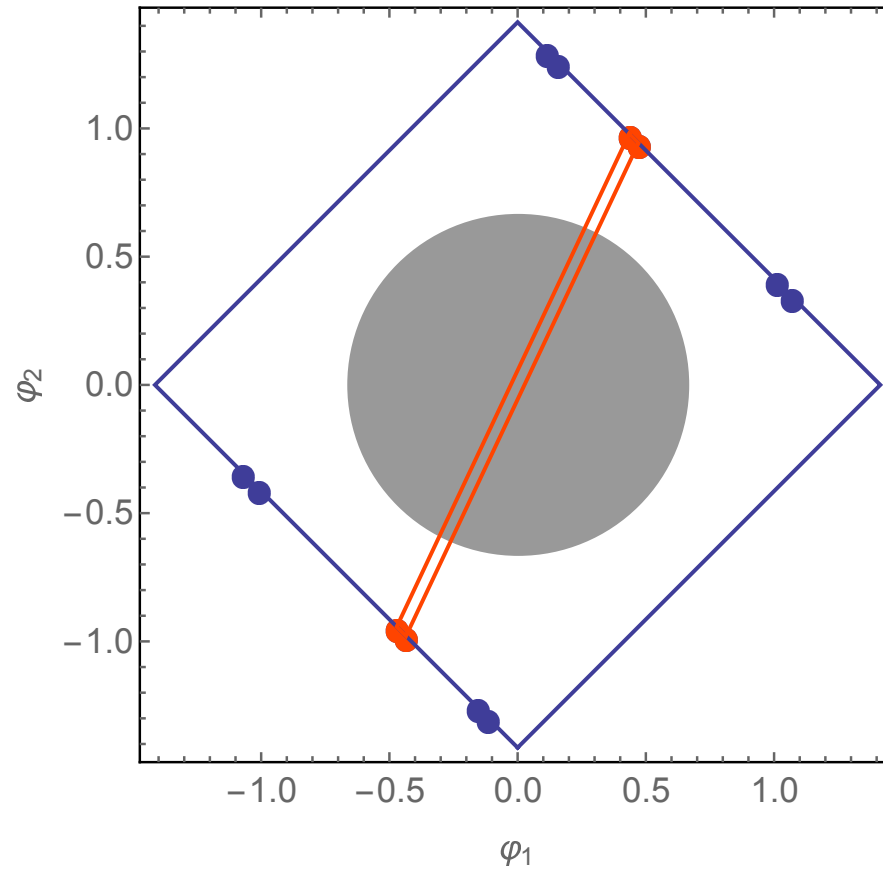
The wiggles in the case of strong alignment

# Weak alignment



The convex hull restrictions are trivially satisfied

# Strong alignment



Subleading terms satisfy the restrictions

# Modulated natural Inflation

It seems plausible that under some circumstances the wiggles become important and

- spoil the flat direction
- provide an upper limit on decay constant  $f_{\text{eff}}$

Explicit calculations are necessary to clarify the situation

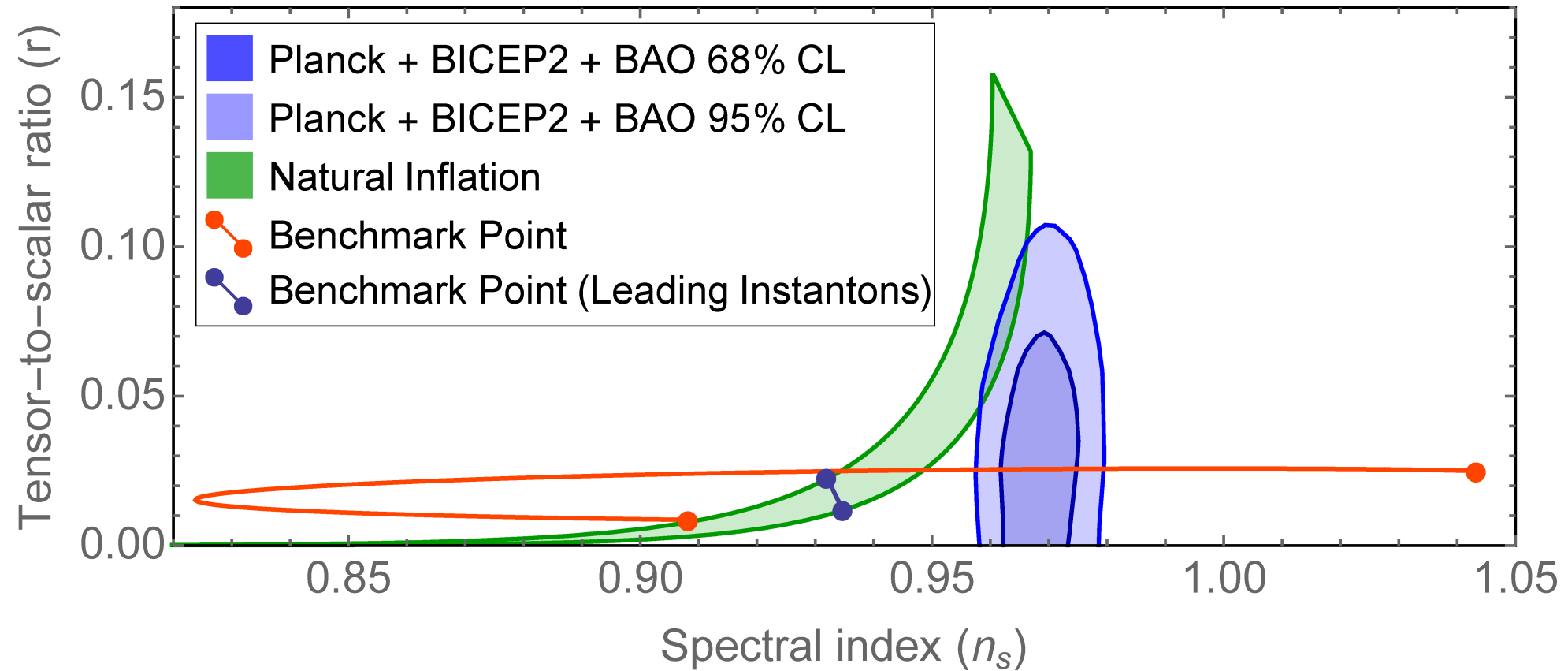
- might be beyond our present capabilities
- observational confirmation is extremely important

Restrictions from WGC are satisfied here both in the aligned **and** non-aligned case.

**WGC appears as a “red herring”**

(Kappl, Nilles, Winkler(2), 2015)

# Modulated natural inflation

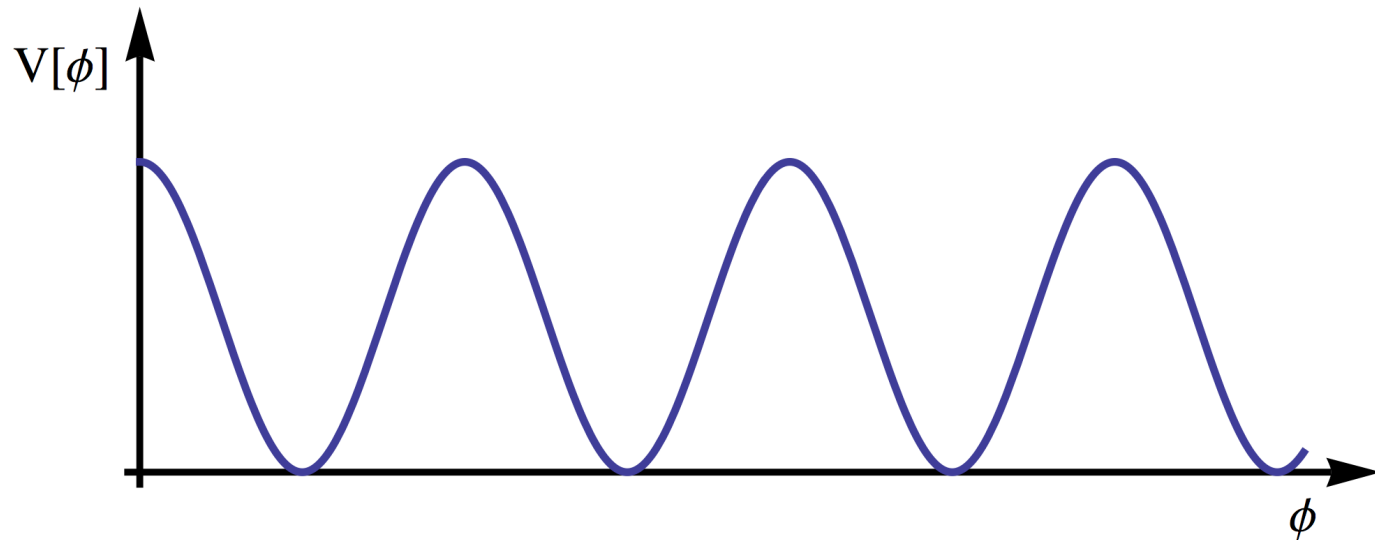


The scalar index shows a large variation

(Abe, Kobayashi, Otsuka, 2015; Kappl, Nilles, Winkler(2), 2015)

# QCD axion and axionic domain walls

In general we have  $a = a + 2\pi N f_a$  for  $V \sim \cos(Na/f_a)$ ,



leading to  $N$  nontrivial degenerate vacua separated by maxima of the potential.

During the cosmic evolution this might lead to the production of potentially harmful axionic domain walls.



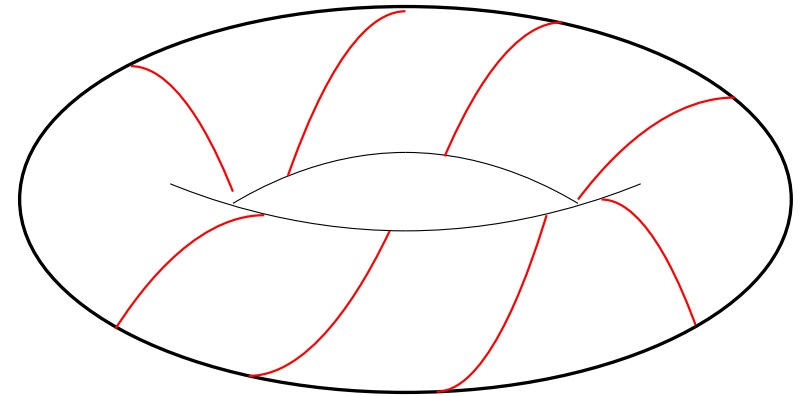
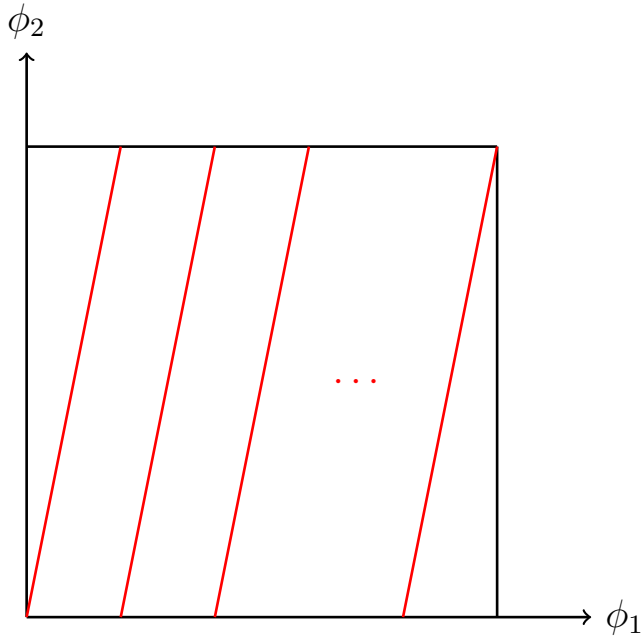
# Two-Axion-model (by Kiwoon Choi)

Consider a system with two axions

$$V \sim \Lambda_1^4 \cos \left( \frac{a_1}{f_1} + N \frac{a_2}{f_2} \right) + m \Lambda_2^3 \cos \left( \frac{a_2}{f_2} \right)$$

- For fixed  $a_1$  there are  $N$  nontrivial vacua and potentially  $N_{\text{DW}} = N$  domain walls
- for  $m = 0$  there is a Goldstone direction,
- and thus a continuous unique vacuum with effective domain wall number  $N_{\text{DW}} = 1$  (Choi, Kim, 1985)
- the Goldstone mode develops an axionic potential in the case  $m \neq 0$

# The axionic vacuum



(Choi, Kim, Yun, 2014)

- There is continuous unique vacuum with effective domain wall number is  $N_{\text{DW}} = 1$  (Choi, Kim, 1985)
- the Goldstone mode develops an axionic potential in the case  $m \neq 0$

# Quintessential axion alignment

Axions could be the source for dynamical dark energy

- in contrast to scalar quintessence, the axion has only derivative couplings and does not lead to a “fifth force”
- we need a slow roll field with  $\Lambda \sim 0.003 \text{ eV}$
- to act as dark energy today we need  $f_a \geq M_{\text{Planck}}$
- the quintaxion mass is  $m_a \sim \Lambda^2 / M_{\text{Planck}} \sim 10^{-33} \text{ eV}$

Again we need a trans-Planckian decay constant for a consistent description of the present stage of the universe

- the problem can be solved via aligned axions à la KNP

(Kaloper, Sorbo, 2006)

# Bottom-up approach

Axions can help with the solution of various problems

- natural inflation
- the strong CP-problem
- pseudoscalar quintessence

In bottom-up approach one aims at a minimal model and thus postulates a single axion field

But there are some remaining problems:

- trans-Planckian decay constants and
- axionic domain walls

require a non-minimal particle content.

# Top-down approach

Possible UV-completions provide new ingredients

- there are typically **many moduli fields**
- axion fields are abundant in string compactifications

No strong motivation to consider **just a single axion field**.  
Additional fields are needed for

- trans-Planckian values for **inflation and quintessence**
- **domain wall problem** of QCD axion
- a simple implementation of **low-scale supersymmetry**

Vielfalt statt Einfalt - Diversity beats Simplicity