Exercises on Elementary Particle Physics II Prof. Dr. H.-P. Nilles

Final exam: Monday July, 10th 2006 from 11.15 to 13.00 in HS1 PI

1. Supergravity definitions

The Kähler potential $K(\Phi^i, \Phi^*_i)$ and the superpotential $W(\Phi^i)$ are combined to

$$G(\Phi^{i}, \Phi_{j}^{*}) = -\frac{K(\Phi^{i}, \Phi_{j}^{*})}{M^{2}} - \log\left(\frac{|W(\Phi^{i})|^{2}}{M^{6}}\right).$$

The F-term part of the scalar potential is given by:

$$V_{\text{scalar}}(\phi^{i}, \phi^{*}_{j}) = -e^{G} \left[3 + G_{k} \left(G^{-1} \right)_{l}^{k} G^{l} \right] M^{4},$$

where ϕ denotes the scalar component of Φ and the derivatives are defined as

$$G_i = \frac{\partial G}{\partial \phi^{*i}}, \quad G^j = \frac{\partial G}{\partial \phi_j}, \quad G_i^j = \frac{\partial^2 G}{\partial \phi^{*i} \partial \phi_j}$$

Furthermore, the F^i component of the chiral superfield Φ^i (for constant gauge kinetic function f_{AB}) reads:

$$F^i = W^i + \frac{1}{M^2} K^i W$$

2. The Polonyi superpotential

Assume a minimal form for the Kähler potential $K(\Phi, \Phi^*) = \Phi^* \Phi$ and the following superpotential

$$W(\Phi) = m^2(\Phi + \beta)$$

with β a dimensionful parameter which we will use later to adjust the vacuum energy to zero.

- (a) Determine the F-term of Φ . For which values of β is SUSY definitely broken?
- (b) For which values of β is there a non-SUSY vacuum with zero energy? Calculate the vev of ϕ at those vacua. Hint: The solution should be $\langle \phi \rangle_{\pm} = \pm (\sqrt{3} - 1)M$ and $\beta_{\pm} = \pm (2 - \sqrt{3})M$.

(c) Calculate the gravitino mass $m_{3/2} = e^{-G/2}M$. Express it in terms of the SUSY breaking scale $M_{\text{SUSY}}^2 = \langle e^{-G/2} (G^{-1})_l^k G_k M \rangle$.